Maize and sunflower biomass estimation in southwest France using high spatial and temporal resolution remote sensing data

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A B S T R A C T

The recent availability of high spatial and temporal resolution (HSTR) remote sensing data (Formosat-2, and future missions of Venus and Sentinel-2) offers new opportunities for crop monitoring. In this context, we investigated the perspective offered by coupling a simple algorithm for yield estimate (SAFY) with the Formosat-2 data to estimate crop production over large areas. With a limited number of input parameters, the SAFY model enables the simulation of time series of green area index (GAI) and dry aboveground biomass (DAM). From 2006 to 2009, 95 Formosat-2 images (8 m, 1 day revisit) were acquired for a 24×24 km² area southwest of Toulouse, France. This study focused on two summer crops: irrigated maize (Zea mays) and sunflower (Helianthus annuus). Green area index (GAI) time series were deduced from Formosat-2 NDVI time series and were used to calibrate six major parameters of the SAFY model. Four of those parameters (partition-to-leaf and senescence function parameters) were calibrated per crop type based on the very dense 2006 Formosat-2 data set. The retrieved values of these parameters were consistent with the in situ observations and a literature review. Two of the major parameters of the SAFY model (emergence day and effective light-use efficiency) were calibrated per field relative to crop management practices. The estimated effective light-use efficiency values highlighted the distinction between the C4 (maize) and C3 (sunflower) plants, and were linked to the reduction of the photosynthesis rate due to water stress. The model was able to reproduce a large set of GAI temporal shapes, which were related to various phenological behaviours and to crop type. The biomass was well estimated (relative error of 28%), especially considering that biomass measurements were not used for the calibration. The grain yields were also simulated using harvest index coefficients and were compared with grain yield statistics from the French Agricultural Statistics for the department of Haute-Garonne. The inter-annual variation in the simulated grain yields of sunflower was consistent with the reported variation. For maize, significant discrepancies were observed with the reported statistics.

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1. Introduction

Soil carbon sequestration has been identified by the Intergovernmental Panel on Climate Change as one of the options for the mitigation of greenhouse gases (Hutchinson et al., 2004). Agricultural lands cover approximately 35% of the land surfaces and through photosynthesis and biomass production, agriculture can act as carbon sinks (Ceschia et al., 2010; Kutsch et al., 2010). However, many factors impact photosynthesis, including crop type, crop management practices, soil properties and climate. Thus, crop production is highly variable in both space and time. This variability should be quantified to improve the management of agricultural lands and to refine regional carbon balance estimates.

Land surfaces have been studied for many years using remote sensing reflectances and vegetation indices (Asrar et al., 1984; Baret & Goutey, 1991; Basso et al., 2001; Bastiaanssen et al., 2000; Duchemin et al., 2008a; Fahve et al., 2004; Moulin et al., 1998; Pinter et al., 2003; Scotford & Miller, 2005). Crop fields of South-West of France are often of small size and they experience high temporal dynamics due to plant growth and management practices (soil tillage, sowing, irrigation and harvest). Remote sensing satellites providing high frequency observations at a high spatial resolution are thus well designed to monitor cropping systems. Until recently, high spatial and temporal resolutions have not been attainable because of technological limitations. Currently, the Formosat-2 Taiwanese satellite has the unique capability of taking daily images at 8 m spatial resolution with a constant viewing angle (Chern et al., 2006). The high temporal resolution of the monodirectional Formosat-2 data allows the acquisition of very accurate surface reflectances and vegetation indices time series (Hagolle et al., 2008, 2010).

Previously, only a small number of agro-meteorological studies have been performed using both high spatial and temporal resolution images
with constant viewing angles such as Formosat-2 data. Duchemin et al. (2008a) have presented a preliminary evidence of the usefulness of such data for land use mapping and agricultural water management for wheat crops in Morocco. Numerous studies (Bsaies et al., 2009; Courault et al., 2008; Fieuzal et al., 2011; Hadria et al., 2010) have shown its utility for capturing the spatiotemporal variability of two key biophysical variables: albedo and green leaf area index. Hadria et al. (2009) have demonstrated the convenience of this type of data for the detection of agricultural operations such as ploughing or irrigation at the beginning of the cropping season. In this study, we analysed the potential for the use of high spatial and temporal resolution images to provide regular estimates of crop production over large areas. We used Formosat-2 data in combination with a simple algorithm for yield estimate (SAFY, Duchemin et al., 2008b).

Crop models were originally designed to simulate crop growth on agricultural fields where soil, climate and agricultural practices were well known and spatially homogeneous. They have been used in a wide range of agro-environmental issues. However, the application of crop models over large areas is still challenging because the soil properties, the climatic variables and the agricultural practices are highly variable in space and time (Boote et al., 1996; Faiivre et al., 2004; Moulin et al., 1998; Wit de et al., 2005). In confronting this challenge, we have distinguished three categories of crop models:

i) Complex models that simulate a large set of agro-environmental variables through the description of numerous coupled physiologically and physiological processes, such as photosynthesis, respiration, evapotranspiration and nitrogen uptake (e.g., AFRC-WHEAT2, CERES, Sirius, SUKROS2, STICS, SWHEAT, see Jamieson et al., 1998 and Brisson et al., 2003 for reviews). These models require a large number of parameters and input data. This information may be available during scientific experiments, or it may be available from some farmers at a local scale, but it is generally not available over large areas.

ii) In contrast, very simple models calculate biomass as an empirical sum of vegetation indices derived from remote sensing observations (Dong et al., 2003; Tucker & Sellers, 1986; Wessels et al., 2006). These models are all based on the light use efficiency (LUE) theory (Monteith, 1977). These models are uncomplicated to parameterise over large areas using time series of remote sensing data with low spatial resolution data acquired at 10-day or monthly intervals. They provide estimates of net primary production for natural ecosystems such as forests (e.g., Dong et al., 2003) or grasslands (e.g., Loseen et al., 1995; Prince, 1991; Tucker et al., 1983; Wylie et al., 1991). However, these models appear less suited for crop monitoring because they do not accurately account for crop type and management (Faiivre et al., 2004).

iii) The third category of crop models gathers the description of the main biophysical processes (biomass accumulation, leaf partition, leaf senescence...), and empirical parameterisations. These models combine the LUE theory with a simulation of the successive plant phenological stages. This semi-empirical approach, in which the number of formalisms and parameters is limited, enables studies over larger areas. Maas (1993) has demonstrated the value of such a model for simulating time series of leaf area index and dryaboveground biomass for maize and wheat crops. Lobell et al. (2003) and Liu et al. (2010), who worked on the combination of such semi-empirical models and remote sensing data, have underlined the need for high temporal and spatial resolution satellite data to improve model predictions.

The SAFY model (Duchemin et al., 2008b) belongs to this third category of semi-empirical models. It was specifically designed for large-scale studies because it describes the main biophysical processes using climatic data. Previous studies have shown that the SAFY model, once calibrated with green leaf area index time series, resulted in accurate estimates of dry aboveground biomass for irrigated wheat cultivated in semi-arid regions (Duchemin et al., 2008a; Fieuzal et al., 2011; Hadria et al., 2009).

The objective of this study was to evaluate the coupling between high spatial and temporal resolutions remote sensing data with a simple crop model to estimate crop production at regional scale. An example is shown using Formosat-2 images combined with the SAFY model applied to sunflower (Helianthus annuus) and maize (Zea mays) in southwest France. The experiment was performed during four successive agricultural seasons (2006–2009) with a focus on maize and sunflower crops, which are the two dominant summer crops cultivated in the southwest of France. Time series of Formosat-2 observations were used to calibrate parameters of the SAFY model over a region covering approximately 600 km². Evaluation of the model used an in situ data set collected from 2006 to 2009 and regional grain yield statistics.

2. Materials and methods

2.1. Study area

The study area is a 24×24 km² area located near Toulouse, in southwest France (1°10′ E, 43°27′ N, Fig. 1). The climate is temperate continental with hot (daily mean temperature approximately 22.5 °C) and dry (38 mm/month of rainfall) summers. Arable lands cover up to 60% of the study area, of which 40% is cultivated during summer, predominantly with irrigated maize (grain and silage) and sunflower crops. The southeastern and the western parts of the study area are hilly landscapes with small fields (approximately 10 ha); the centre of the study area, near the Garonne River, is nearly flat with larger fields (approximately 25 ha).

In the study area, maize fields are sown from mid-April to beginning of June, and last until September–October. Most of maize fields are irrigated during hottest month (July and August). Sunflower fields are sown from end of March to end of June and are mainly non-irrigated.

2.2. Field data

The study was performed during from 2006 to 2009 on maize and sunflower crops. Four types of in situ data were measured: the dry aboveground biomass (DAM), the specific leaf area (SLA), the green area index (GAI) and the fraction of absorbed photosynthetically active radiation (FAPAR). The DAM and the SLA were estimated with a destructive method. The GAI and the FAPAR were estimated from hemispherical photographs.

The main characteristics of the field measurements are shown in Fig. 1 and Table 1. Two protocols were used to collect the data:

(i) Transect sampling protocol: the measurements of DAM were performed from 2006 to 2008 along two transects crossing the field. This protocol was applied in two fields belonging to the CarboEurope-IP Regional experiment (Dolman et al., 2006). These two fields are hereafter referred to as “Lamothe” and “Auradé”. They belong to an experimental farm managed by the Purpan Engineering School and to a farmers association (http://www.agriculteurs-aurade.fr/). Thirty plants were harvested 6 to 9 times per growing season (Table 1). For each plant, leaf biomasses were measured independently and leaf areas were measured using a planimeter (Licor 3100 Lincoln Inc., Nebraska) in order to derive the specific leaf area (SLA).

(ii) Elementary sampling unit (ESU) protocol: the measurements of DAM, GAI and FAPAR were performed within a 20 m sided square area. Eleven fields located near the “Lamothe” farm were sampled (back squares in Fig. 1 and Table 1). These fields are hereafter referred to as the ESU fields. The locations of the ESUs were recorded with a GPS. GAI and FAPAR were measured in 2008 using digital
hemispherical photographs (DHPs). Each ESU was sampled with 13 DHPs applying the VALERI spatial sampling protocol (http://w3.avignon.inra.fr/valeri). The in situ data were collected 7 to 10 times during the growing season, yielding to 23 GAI and FAPAR estimations for maize and 19 for sunflower (Table 1). The DAM was estimated from 10 plants collected near the ESUs in 2008 and 2009, leading to 14 DAM estimations for maize and 11 for sunflower. In 2009, only one biomass measurement was performed per ESU during the growing season.

The concept of green area index (GAI, Baret et al., 2010) corresponds to the photosynthetically active plant area without organ distinctions. It is related to FAPAR and can be derived from DHPs. In our study, the DHPs were taken with a Nikon CoolPix 8400 camera equipped with a FC-E8 fisheye lens. The camera was put at the top of a pole to keep the viewing direction (looking downward) and the canopy-to-sensor distance constant (~1.5 m) throughout the growing season. This protocol allowed the reduction of errors in the directional gap fraction estimates and thus in the FAPAR and GAI estimates (Demarez et al., 2008). The DHP were processed using CAN-EYE V5 (http://www4.paca.inra.fr/can-eye), which provides estimates of the daily FAPAR and of the “effective” and “true” GAI (Baret et al., 2010; Demarez et al., 2008). In this study, we used the effective GAI (GAIeff,CAN-EYE), which is highly correlated with remote sensing observations and the daily FAPAR (FAPARDaily,CAN-EYE).

In addition to these measurements, several farmers provided grain yield estimates for maize (4 estimates) and sunflower (37 estimates) for 12 fields located near Lamothe and for 16 fields located near Auradé.

2.3. Meteorological data

Meteorological data were generated by the mesoscale atmospheric analysis system SAFRAN, which is operational at Météo-France (Durand et al., 1993). Among other variables, SAFRAN simulates air temperature at 2 m above the ground (Ta), incoming global radiation (Rg) and precipitation (P) based on a combination of measurements (weather stations) and modelling. The data are available every 6 h over a grid with an 8 km spatial resolution (plus symbols in Fig. 1).

The SAFRAN meteorological variable data were processed to compute daily mean Ta and cumulated daily Rg and P for each Formosat-2 pixel (8 m) of the study area. The spatial oversampling was performed using a bilinear spatial interpolation. The evaluation performed by Quintana-Segui et al. (2008) all over the France have shown that Rg (RRMSE = 60%) and Ta (RRMSE = 13%) are accurately estimated by SAFRAN, while the accuracy of P was found lower (RRMSE = 100%), especially in mountainous areas.

The analysis of the meteorological variables over the Formosat-2 footprint revealed differences between the years. The driest and hottest years were 2006 and 2009; the cumulated daily precipitation for the summer growing season, from DoY (day of year) 125 to 250, was 147 mm in 2006 and 152 mm in 2009, whereas it reached

Fig. 1. The study area as observed in a Formosat-2 image in July 2008. The areas where field data were collected are shown in a) and b) frames; the black symbols indicate the locations of the elementary sampling units (11 ESUs near Lamothe), and the blue disks indicate the fields for which the farmers provided grain yield data (12 fields near Lamothe, 16 fields near Auradé). The so-called Lamothe (frame c) and Auradé (frame d) fields (delimited with black lines) are experimental fields that belong to the CarboEurope-IP experiment; biomass measurements were performed along transects (in yellow). Black crosses indicate the SAFRAN meteorological grid. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 1

<table>
<thead>
<tr>
<th>Crop type</th>
<th>Year</th>
<th>GAI/FAPAR</th>
<th>DAM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maize</td>
<td>2006</td>
<td>ESU (3): 23</td>
<td>Lamothe: 6</td>
</tr>
<tr>
<td></td>
<td>2008</td>
<td>ESU (1): 9</td>
<td>Lamothe: 6</td>
</tr>
<tr>
<td>Sunflower</td>
<td>2009</td>
<td>ESU (5): 5</td>
<td>Lamothe: 6</td>
</tr>
<tr>
<td></td>
<td>2007</td>
<td>ESU (2): 2</td>
<td>Auradé: 7</td>
</tr>
<tr>
<td></td>
<td>2008</td>
<td>ESU (2): 9</td>
<td>Auradé: 7</td>
</tr>
<tr>
<td></td>
<td>2009</td>
<td>ESU (2): 2</td>
<td>Auradé: 7</td>
</tr>
</tbody>
</table>
248 mm in 2008 and 273 mm in 2007. The cumulated air temperature during the same period was approximately 2570 °C in 2006 and 2009 and approximately 2370 °C in 2007 and 2008.

2.4. Formosat-2 data

Formosat-2 is a high spatial (8 m) and temporal (daily revisit time) resolution satellite with four spectral bands (488, 555, 650 and 830 nm) and a 24 km field of view (Chern et al., 2006). Formosat-2 takes images at a constant viewing angle. Ninety-five images were taken of our study area from 2006 to 2009 (Fig. 2). In 2006, the images were scheduled at a high priority level with a nominal time step of 3 days. The 2006 data set contained 51 images, including 27 images that were almost totally cloud-free. After 2006, only images with a cloud cover less than 20% were purchased. Thus, 14 images were available in 2007, 11 images in 2008 and 19 in 2009. In 2008, no cloud-free images were available from February 11 to June 19.

All of the Formosat-2 images were pre-processed for geometric, radiometric and atmospheric corrections and the filtering of clouds and shadows (Hagolle et al., 2008, 2010). This processing resulted in surface reflectances images and associated cloud-masks. The absolute location accuracy was 0.4 pixels, i.e., 3.2 m (Baillarin et al., 2008), which is quite satisfactory with respect to both the field and ESU sizes.

2.5. Land cover

Maize and sunflower were identified using classification and segmentation methods applied to Formosat-2 surface reflectances images. This processing was performed each year using all images acquired from January to December. The classification method was performed using a fuzzy contextual algorithm of the Iterative Conditional Mode type based on a Markovian model (Idbraim, 2009). The segmentation algorithm was based on a watershed method (Fjortoft et al., 1999) and lead to homogenous units (called HU hereafter), corresponding to homogenous radiometric zones. The parameters used for the segmentation were chosen such that the agricultural fields were split in the case of high intra-field variability. As a result, an agricultural field corresponded to one or several HU (see Fig. 3). Only HU larger than 640 m² (10 Formosat-2 pixels) were considered in this study.

Each year, this processing provided 40 land use classes, from which maize (grain and silage) and sunflower were extracted. The analysis of the mapped HU showed that:

(i) Sunflower and maize crops covered approximately 21% of the study area.

(ii) Maize was primarily cultivated in the centre of the Formosat-2 images, near the Garonne River. It covered approximately 7700 ha in 2006, 6500 ha in 2007, 7400 ha in 2008 and 6600 ha in 2009. The maize crops were segmented into HU of 2 ha on average. Approximately 95% of these HU were identified as grain maize, the remaining 5% being silage maize.

2.6. Time series of Green Area Index (GAI)

Many studies have demonstrated the link between spectral vegetation indices (e.g., NDVI, SAVI and EVI) derived from remote sensing observations and the green leaf area index (e.g., Colombo et al., 2003; Duchemin et al., 2006; Myneni & Williams, 1994; Walthall et al., 2004; Weiss et al., 2002). In our study, the green area index (GAI\textsubscript{eff,F2}) was estimated from the Formosat-2 images using the NDVI and the following exponential relationship (Eq. (1)):

\[
\text{GAI}_{\text{eff,F2}} = k_1 \times e^{k_2 \times \text{NDVI}} - k_3
\]  

The coefficients of Eq. (1) were estimated using the minimisation of the root mean square error (RMSE) between GAI\textsubscript{eff,CAN-EYE} estimated from the DHPs from the ESUs and GAI\textsubscript{eff,F2} estimated from Eq. (1). The GAI\textsubscript{eff,CAN-EYE} measurements taken more than 4 days after or before the Formosat-2 acquisitions were eliminated from the data set. The NDVI-GAI\textsubscript{eff,CAN-EYE} scatterplot is presented in Fig. 4. A single relationship (the black line in Fig. 4) was used for both crops (coefficients \( k_1 = 0.35, k_2 = 2.86, k_3 = 0.24 \) in Eq. (1)). The RMSE between GAI\textsubscript{eff,CAN-EYE} and GAI\textsubscript{eff,F2} was equal to 0.38 m².m⁻² and the relative RMSE (RRMSE) was equal to 20%. The formulation of the equation differed from more commonly used logarithmic formulation. Nevertheless, the current formulation fitted correctly with the in situ measurements of effective GAI. With the current set of coefficients, the GAI estimate could not
exceed 5.9 m².m⁻², which was sufficient as it corresponded to effective GAI.

This relationship was then applied to all Formosat-2 pixels. This processing resulted in a time series of effective Formosat-2 GAI (called hereinafter GAIₑ₂), which were spatially averaged over the HU labelled as maize (silage or grain) and sunflower. During the calculation, all of the data with cloudy or shadowed pixels were excluded.

2.7. Calibration of the SAFY model

The simple algorithm for yield estimates (SAFY) is a daily time step model that simulates time series of leaf area index and dry aboveground biomass from the air temperature and the global incoming radiation. An overview of the model is provided in Appendix A; a full description is available in Duchemin, Maisongrande, Boulet and Benhadj (2008).

The model was parameterised for each HU labelled as maize (silage or grain) or sunflower using meteorological data derived from SAFRAN. The thirteen parameters of the SAFY model are listed in Table 2. Initial values were put based on a literature review and field measurements for eight parameter and the six major parameters, identified by Duchemin, Maisongrande, Boulet and Benhadj (2008), were calibrated using time series of green area index derived from Formosat-2 images (GAIₑ₂).

2.7.1. Calibration of parameters through literature review and field measurements

The common value of 0.48 was used for the climatic efficiency (Varlet-Grancher et al., 1982). As in Duchemin et al. (2008b), the initial dry aboveground biomass was set arbitrarily to correspond to effective Formosat-2 NDVI. GAIₑ₂, CAN-EYE were collected per ESU and NDVI were averaged on a 3 × 3 pixels windows centred on the ESU. Pluses and circles indicate maize and sunflower crops, respectively.

2.7.2. Calibration of parameters based on remote sensing data

The remaining parameters (Pla, Plb, Stt, Rs, D0 and ELUE) were all retrieved using GAIₑ₂ time series derived from Formosat-2 images. To limit compensation during the optimisation procedure (see Duchemin et al., 2008b), we classified the parameters in two groups: crop-specific and field-specific parameters. Two corresponding phases were used for the calibration. The methodology of the calibration is described in the Fig. 5. The four crop specific parameters (Pla, Plb, Stt, Rs), which constrain the shape of the GAIₑ₂ time course, were calibrated, on phase 1, separately for sunflower, grain maize and silage maize. The two field specific parameters (D0 and ELUE) were calibrated, on phase 2, for each HU.

Prior to the calibration procedure, a delimitation of the growing period was needed (Fig. 6). The day of maximum GAIₑ₂ (DoY 218 in Fig. 6) was first identified. Then, the algorithm seeks backward and forward from this day to determine the starting (DoY 156 in Fig. 6) and ending (DoY 288 in Fig. 6) of the growing period. The GAIₑ₂ values that did not belong to the identified growing period were excluded (plus symbols in Fig. 6).

The calibration of SAFY was then performed by minimising the Root Mean Square Error (RMSE) between the “cleaned” GAIₑ₂ time series and the GAI simulated by SAFY. The minimisation procedure was based on an adapted version of the simplex method (Lagarias et al., 1998), which was run 50 times with a random determination of initial values to avoid stops in local minima. Intervals of acceptable values were defined for each parameter (Table 2). These intervals were constant for all of the parameters except the date of emergence, for which the interval was established independently for each HU to plus or minus 20 days around the start of the growing period.

The crop-specific parameters were estimated, on phase 1 of the calibration (see Fig. 5), using the 2006 Formosat-2 data set. This data set was preferred as it contained a high number of images regularly distributed during the whole growing season. This lead to 6032 GAIₑ₂
time series computed from the HU. Depending on the HU, 18 to 28 cloud-free images were available from May to September. HU with maximum GAIF2 less than 1 m<sup>-2</sup> or that lead to RMSE superior to 0.38 m<sup>-2</sup> were not kept in our analysis as they were considered to be incorrectly classified. However, an important set (5721) of crop-specific parameters (Pla, Plb, Stt, Rs) was available for each crop: 1980 for grain maize, 97 for silage maize and 3644 for sunflower. A median value was then computed for each crop and used on phase 2 of the calibration (see Fig. 5) to estimate the field-specific parameters (ELUE and D<sub>0</sub>). They were estimated per year and per different spatial units (fields, transect and ESU) to allow comparison with in situ data.

The minimisation procedure of phase 2 was based on a regular simplex method because there is no compensation between these two parameters (Duchemin et al., 2008b).

3. Results and discussion

In this section, results of the calibration and the validation are discussed. The two parameters, estimated from in situ measurements are first discussed. The parameters, estimated from the GAIF<sub>2</sub> are then described: crop-specific (Pla, Plb, Stt and Rs) and field-specific (ELUE and D<sub>0</sub>). Finally, the validations at local and regional scales are described in the two last sections.

3.1. Light-extinction coefficient and Specific Leaf Area

Fig. 7 displays the relationship between the fraction of absorbed photosynthetically active radiation (FAPAR<sub>CAN-EYE</sub>,daily) and the effective green area index (GAI<sub>CAN-EYE,eff</sub>). A single relationship was used for both crops. The best agreement was obtained using a light-extinction coefficient (K<sub>ext</sub>) of 0.63 (see Eq. (5) in Appendix A). The RMSE between FAPAR derived from this relationship and FAPAR<sub>CAN-EYE,daily</sub> was 0.033.

The relationship between the leaf area and leaf mass is displayed in Fig. 8. These two variables were linearly related. SLA values corresponding to the slopes of the relationships (Fig. 8) were used in the SAFY simulations: 0.012 m<sup>2</sup>g<sup>-1</sup> for sunflower and 0.024 m<sup>2</sup>g<sup>-1</sup> for maize.
They thus exhibited larger variations in the GAI F2 time series. Spatial distribution of rainfall and to soil water content than maize. Sunflower appeared more scattered for sunflower occurring during the minimisation procedure. The parameters part of this scattering may be due to parameter compensations very scattered. As previously suggested by Duchemin et al. (2008b), median values are reported in Table 2 and the distributions appeared applied on the 5721 HU of the 2006 Formosat-2 data set. Their destructive measurements. Pluses and circles indicate maize and sunflower crops, respectively. The slopes of the solid lines correspond to the SLA (m².g⁻¹) values.

3.2. Crop-specific parameters

Fig. 9 shows the box and whiskers plots of the distributions of the crop specific parameters (Pla, Plb, Stt and Rs) for maize (grain: M and silage: SM) and sunflower (SF) based on phase 1 of the calibration applied on the 5721 HU of the 2006 Formosat-2 data set. Their median values are reported in Table 2 and the distributions appeared very scattered. As previously suggested by Duchemin et al. (2008b), part of this scattering may be due to parameter compensations occurring during the minimisation procedure. The parameters appeared more scattered for sunflower than for maize likely because sunflower crops, that are not irrigated, are much more sensitive to the spatial distribution of rainfall and to soil water content than maize. They thus exhibited larger variations in the GAI F2 time series.

“Typical” maize (grain and silage) and sunflower GAI F2 time series computed from three HU of the 2006 Formosat-2 data set are plotted on Fig. 10. The analysis of Figs. 9, 10 and Table 2 revealed that significant information could be derived from the distributions of the crop specific parameters:

(i) The dry aboveground biomass allocated to the leaf at plant emergence (1−Pla) was 65% for grain maize, 66% for silage maize and 84% for sunflower (Fig. 9). These values were consistent with the ratios of the leaf mass to the dry aboveground biomass derived from in situ measurements at the beginning of the agricultural season, which were 75% for maize (Lamothe in 2006) and 83% for sunflower (Auradé in 2007). (ii) No significant difference was observed between the grain and silage parameters, except the rate of senescence (Rs in Table 2), which was approximately 15 times higher for silage maize. This very high rate of senescence for silage maize corresponded with the sudden drop of GAI F2 due to harvesting as illustrated in Fig. 10. Silage maize is used to feed animals and thus it is harvested earlier than grain maize, when grain humidity reaches 80%. (iii) Senescence began earlier for sunflower than for maize. The threshold of cumulated temperature to initiate senescence was estimated to be 70% lower for sunflower than for maize (Stt in Table 2). This difference is well illustrated in the GAI F2 time series (Fig. 10) and was previously shown by Andrade (1995).

3.3. Field specific parameters

The cumulated distribution of the effective light-use efficiency (ELUE) and the emergence dates (Do) estimated for the sunflower and maize crops of the Formosat-2 footprint are presented in Fig. 11 (a to d). Numbers of HU used to compute the cumulated distribution are shown in the Fig. 11 (a and b). The cumulated distributions of the maximum GAI (GAI max), the rainfall and the temperature stress factor are also plotted (Fig. 11 e to j). The rainfall was cumulated from 30 days before emergence to senescence. The temperature stress factor corresponds to the average of the FT function (Eq. (3) in Appendix A) from emergence to senescence.

The median value of the ELUE averaged over the four years was 3.3 gMJ⁻¹ for maize (Fig. 11a) and 2.0 gMJ⁻¹ for sunflower (Fig. 11b). The SAFY model thus appeared adequate to reproduce the basic difference in photosynthetic rate between maize (C4 plant) and sunflower (C3 plant). The ELUE values for sunflower increased from 2006 to 2008 in relation with increasing values of GAI max (Fig. 11f). A similar positive correlation was observed between the median values of cumulated rainfall (Fig. 11g) and GAI max. This reveals that the lack of rainfall, inducing water stresses, reduced the GAI max values leading thus
to low ELUE values. In contrast, the maize inter-annual variation of 
\( \text{GAI}_{\text{max}} \) and thus ELUE were not related to the rainfall. This is consistent 
as maize is irrigated to avoid water stress. On the contrary, \( \text{GAI}_{\text{max}} \) values of maize are more related to temperature stresses factor (\( F_T \), Fig. 11i). Two groups were highlighted: 2006/2009 (high \( F_T \) and high \( \text{GAI}_{\text{max}} \)) and 2007/2008 (low \( F_T \) and low \( \text{GAI}_{\text{max}} \)). In 2009, the \( \text{GAI}_{\text{max}} \) 
(Fig. 11e) values were similar to those of 2006 despite lowers temperatures inducing higher temperature stress factors (Fig. 11i). However, the ELUE values were higher in 2009. Indeed, as GAi values were similar in 2009 and 2006, the calibration procedure lead to highest 
ELUE values in 2009 (Fig. 11a) to compensate the limiting effect of low 
temperatures. The same trend was observed when comparing 2007 and 
2008. These results revealed that: (i) the \( \text{GAI}_{\text{max}} \) and ELUE seem to be a 
good indicator of water stresses for non-irrigated sunflower; (ii) the 
combination ELUE/ \( \text{GAI}_{\text{max}} \) seem to be a good indicator of temperature 
stresses for irrigated maize.

The emergence dates (\( D_0 \)) were also significantly different between 
maize (Fig. 11c) and sunflower (Fig. 11d). For maize, the median value 
was stable over the years and was approximately 164 (June, 13). The 
plant emergence always occurred within a limited time period; each

Fig. 10. Example of three 2006 Formosat-2 GAi time series. Red pluses, blue crosses and green circles indicate grain maize, silage maize and sunflower, respectively. Full lines show the SAFY simulations. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 11. Cumulative distribution function (CDF) of ELUE (a and b), \( D_0 \) (c and d) and maximum GAi (\( \text{GAI}_{\text{max}} \), e and f) simulated for maize (left column) and sunflower (right column)
in 2006 (black), 2007 (red), 2008 (green) and 2009 (blue) over the whole Formosat-2 footprint. The rainfall (g and h) was cumulated from 30 days before emergence to the start of the senescence. The mean temperature stress (i and j) was cumulated from emergence to the start of the senescence. The amount of data used is shown in a and b. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
year, 90% of all of the D0 values were within +/- 15 days of the annual median value. For sunflower, D0 was more variable and 90% of the D0 values were within +/- 45 days of the annual median value. This was consistent with the crop managements as maize is irrigated contrary to sunflower. Sunflower crops are thus more sensitive to rainfall occurrences and soil properties leading to higher spatial and temporal variability.

3.4. Evaluation of the simulated GAI and DAM time series at local scale

A quantitative evaluation of the model was performed by comparing the dry aboveground biomass (DAM) simulated by SAFY with those estimated from field measurements. The spatial pattern used for the validation corresponded to the pixels of the footprint of in situ data: transect, ESU and field. The model was calibrated using the GAI[F2] time series averaged over the pixels that encompassed transects (sunflower at Auradé in 2007 and maize at Lamothe in 2006 and 2008), over a 3 x 3 pixel window centred on the ESUs (2008 and 2009) or over the pixels that encompassed fields where grain yields were collected. The GAI[F2] and DAM time series from 2006 to 2008 resulting from this processing are displayed in Fig. 12.

The analysis of the simulated GAI time series confirmed that the SAFY model was able, after calibration, to reproduce the large set of GAI[F2] time series. The maximum GAI[F2] values of maize were quite low (<3.5 m²·m⁻²), which is expected as effective values are proven to underestimate destructive values. This underestimation could reach 30% for the maize and 16% for the sunflower as shown by Demarez et al. (2008). The continuous GAI increase during leaf growth appeared to be accurately reproduced for all of the crops. The difference observed in the time duration of maximal GAI between the sunflower and the maize is also well reproduced. Finally, the GAI decrease during the senescence period was correctly simulated for all crops except for the sunflower crop in 2008 (case 6, Fig. 12); the observed sudden decrease was not simulated by the SAFY model. Hemispherical photographs (Fig. 13) taken in 2008 on July 17 and 24 (referred to as A and B in Fig. 12) revealed that the NDVI and GAI decrease corresponded with flowering.

The temporal dynamics of DAM were correctly reproduced in most of cases. Most of the simulated values ranged within the

<table>
<thead>
<tr>
<th>Year</th>
<th>Field Type</th>
<th>RMSE [m²·m⁻²]</th>
<th>RMSE [kg·m⁻²]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-2006-SM</td>
<td>0.19</td>
<td>0.19 kg·m⁻²</td>
<td></td>
</tr>
<tr>
<td>2-2008-SM</td>
<td>0.34</td>
<td>0.104 kg·m⁻²</td>
<td></td>
</tr>
<tr>
<td>3-2008-GM</td>
<td>0.26</td>
<td>0.123 kg·m⁻²</td>
<td></td>
</tr>
<tr>
<td>4-2007-SF</td>
<td>0.09</td>
<td>0.119 kg·m⁻²</td>
<td></td>
</tr>
<tr>
<td>5-2008-SF</td>
<td>0.24</td>
<td>0.235 kg·m⁻²</td>
<td></td>
</tr>
<tr>
<td>6-2008-SF</td>
<td>0.32</td>
<td>0.125 kg·m⁻²</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 12. Green area index (GAI) and dry aboveground mass (DAM) simulated (lines) and measured (disks) over 6 experimental fields for the period 2006–2008. M: maize, SM: silage maize and SF: sunflower. Grey error bars on GAI and DAM correspond to the standard deviation computed from the pixels (GAI) and the measurements (DAM) performed either over the transects (cases 1, 2 and 4) or the ESUs (case 3, 5 and 6). A and B, mentioned for case 6, refer to the hemispherical photographs shown in Fig. 13.

Fig. 13. Hemispherical photographs taken in 2008 on July 17 (A) and July 24 (B) over the ESUs corresponding to case 6 of Fig. 12.
and an error (RMSE) of 0.21 kg.m\(^{-2}\) sun removed, the maximum DAM would be underestimated by approximately 29% in relative terms. However, some discrepancies were noted:

(i) In 2008, the maximum DAM produced by the grain maize (case 3, Fig. 12) was underestimated by approximately 29% in relative terms. The deviation may be explained by the lack of consideration of an increase of the light use efficiency (LUE) allocated to shoot biomass at the end of the cycle, due to the cessation of root growth. At the opposite, the simulated LUE (F\(T\) × ELUE) decreases from September as the air temperature decreases, suggesting that F\(T\) is overestimated. If F\(T\) is removed, the maximum DAM would be underestimated by approximately 17% in relative terms.

(ii) Contrary to the maize, the maximum DAM produced by sunflower (cases 4 and 6 in Fig. 12) were overestimated. The maximum dry aboveground biomass was unfortunately not measured for case 5. Recent work by Lecoeur et al. (2011) performed with similar sunflower varieties showed that ELUE decreases from the flowering phase, probably in favour of lipids production. The slight decrease in DAM observed before senescence in the measured biomass was due to measurement errors.

The global comparison between simulated and measured DAM from 2006 to 2009 is presented on Fig. 14 and Table 3. There is a good agreement between simulations and field measurements, with a high correlation \(r^2 = 0.92\), p-value < 0.001, almost no bias \((- 0.02 \text{ kg.m}^{-2})\) and an error (RMSE) of 0.21 kg.m\(^{-2}\). The correlation is higher for silage maize \(r^2 = 0.96\); RRMSE = 11% than for grain maize \(r^2 = 0.86\); RRMSE = 26% and sunflower \(r^2 = 0.78\); RRMSE = 39%. The global accuracy of simulations (RRMSE = 28% on Fig. 14) was satisfactory considering that the most sensitive parameters of the model were only calibrated with remote sensing observations. This accuracy was comparable to that of studies using more complex models with a large in situ data set. They found accuracy of 14% and 32% for maize using SWATRER-SUCROS and CERES (Xevi et al., 1996), 16% using STICS (Brisson et al., 2002) and 23% using EPIC (Cabelguenne et al., 1999). An accuracy of 21% was found for sunflower using EPIC (Cabelguenne et al., 1999).

The SAFY model was also run for fields for which farmers provided grain yields. The in situ grain yields were compared with the maximum simulated DAM (Fig. 15). The data for sunflower were highly scattered. This was partially due to the overestimations of the SAFY biomass and partially due to uncertainties in the in situ grain yields. For maize, too few measurements were available to exhibit a trend. Despite these limitations, a mean harvest index (HI) was computed for each crop as the ratio of in situ grain yields to the maximum DAM. This index was 0.48 for grain maize and 0.25 for sunflower. The HI calculated for maize appeared consistent with those from previous experimental or modelling studies; Cabelguenne et al. (1999) reported a value of 0.5. Due to the SAFY biomass overestimation, the HI calculated for sunflower was very low compared with the in situ values given by Casadebaig (2008), which varied between 0.35 and 0.45.

### Table 3

<table>
<thead>
<tr>
<th></th>
<th>Maize</th>
<th>Sunflower</th>
<th>All crops</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>26</td>
<td>18</td>
<td>44</td>
</tr>
<tr>
<td>RMSE (kg.m(^{-2}))</td>
<td>0.252</td>
<td>0.145</td>
<td>0.215</td>
</tr>
<tr>
<td>Bias (kg.m(^{-2}))</td>
<td>-0.070</td>
<td>0.049</td>
<td>-0.021</td>
</tr>
<tr>
<td>(r^2)</td>
<td>0.91</td>
<td>0.78</td>
<td>0.92</td>
</tr>
</tbody>
</table>

Fig. 14. Comparison between the simulated and measured dry aboveground mass (DAM) over all of the experimental fields for the period 2006–2009.

3.5. Evaluation of the simulated DAM and grain yield over the Formosat-2 footprint

The distributions of the maximum aerial dry biomass (DAM\(_{\text{max}}\)) estimated over the whole Formosat-2 footprint are presented in Fig. 16. For sunflower, the maximum DAM values (Fig. 16b) were reached during the wettest year (2008, Fig. 11h). In 2007, despite the strong rainfall, the DAM\(_{\text{max}}\) values were not as high as in 2008. In 2007, we noticed that the period of emergence was quite long, up to 200 days (Fig. 11d). This was due to heavy rains during the spring, which limited plant emergence, particularly in clay soils, and thus limited the crop production. For maize, the highest maximum DAM values were reached during the hottest years (Fig. 11i).

Fig. 15. Relationship between simulated maximum dry aboveground mass (DAM\(_{\text{max}}\)) and grain yields in 2006, 2007 and 2008, provided by farmers for 28 maize (+) and sunflower (o) crops. The slopes of the dashed lines correspond to the mean harvest index.

The DAM\textsubscript{max} values averaged over four years were equal to approximately 19.5 t.ha\textsuperscript{-1} for maize and 9.6 t.ha\textsuperscript{-1} for sunflower. The grain yields calculated from these averaged DAM\textsubscript{max} values using the harvest index previously estimated (0.48 for maize and 0.25 for sunflower) were 10.1 t.ha\textsuperscript{-1} for maize and 2.4 t.ha\textsuperscript{-1} for sunflower and were in agreement with the values given by the French Agricultural Statistics for the whole department of Haute-Garonne, which were 10.2 t.ha\textsuperscript{-1} for maize and 2.3 t.ha\textsuperscript{-1} for sunflower (Fig. 17, Agreste, 2011). The accuracy of the sunflower grain yield estimation was due to compensation between the overestimated biomass and the underestimated harvest index. Nevertheless, the inter-annual variations of the estimated sunflower grain yields were highly correlated with the reported statistics (\(r = 0.97\), p-value < 0.03, Fig. 17). The lowest simulated grain yields were found in 2006 which was the driest year (Fig. 11b) like in the reported statistics; the highest simulated grain yields were found in 2008 which was the wettest year like in the reported statistics.

In contrast with sunflower, the inter-annual variation in the maize grain yields did not match the reported grain yield statistics (\(r = -0.81\), Fig. 17). The lowest simulated grain yields were found in 2008, which was the year with the highest reported grain yields. The highest simulated grain yields were estimated for 2009, which had the lowest reported grain yields. As discussed previously, there was a clear effect of temperature on maize leaf and biomass production. We may notice that the reported statistics are given for the entire department of Haute-Garonne, which covers an area much larger than the Formosat-2 footprint. In contrast with the sunflower crops, which are mainly located in the northern part of the department, the maize crops are distributed throughout the department, which exhibits a strong spatial gradient in air temperatures. The mean air temperatures were cumulated during the growing period using the SAFRAN data. They varied from 2419 °C (in 2007) to 2646 °C (in 2006) in the northern part of the department and from 2001 °C (in 2007) to 2202 °C (in 2006) in the southern part of the department. The differences observed in cumulative temperature between the northern and the southern part of the department could reach 400 °C. The Formosat-2 footprint was located in the northern part of the department with a cumulative air temperature varying from 2353 °C (in 2007) to 2600 °C (in 2006). Thus, the SAFY simulations performed over the maize crops were considered to not be representative of the entire department of Haute-Garonne and thus unfortunately not comparable with the reported statistics.

4. Conclusion

In this study, we evaluated the combined use of high spatial and temporal resolutions remote sensing data and a simple crop model to estimate maize and sunflower crops production. A semi-empirical crop model (SAFY, Duchemin et al., 2008b) was calibrated with high temporal and spatial resolution Formosat-2 data available from 4 years (2006 to 2009). The results revealed that the high temporal frequency of the 2006 Formosat-2 time series appeared to be mandatory to calibrate 4 of the 13 parameters of the SAFY model (\(P_{a}, P_{b}, S_{t},\) and \(R_s\)), which are crop dependent. Once calibrated, these parameters were used to calibrate effective light-use efficiency (ELUE) and emergence dates (\(D_0\)), and to simulate biomass from 2006 to 2009. From 2007 to 2009, fewer images were available, but the method remained robust because it relied on the pre-calibration
of the phenological parameters using the 2006 high temporal resolution data set. Analysis of the ELUE values showed that the SAFY model was able to reproduce the basic difference in photosynthetic rate between maize (C4 plant) and sunflower (C3 plant). The results also showed that the maximum \( G_{A1} \) value was a good indicator of the canopy water stress for non-irrigated crops such as sunflower. The simulation of \( D_0 \) revealed higher temporal variability for non-irrigated crops. The SAFY model was also able to reproduce the temporal variability of \( G_{A1} \) shape and dry aboveground biomass through the 4 studied years. The errors retrieved from the comparison between destructive sampling and simulated biomass were consistent (RMSE = 0.22 kg.m\(^{-2}\); RRME = 29%) in comparison with the values given by authors who used more complex models. However, this approach faced some limitations. First, the use of the 2006 Formosat-2 data set to calibrate phenological parameters (Pla, Plb, Stt and Rs) might be a potential source of error. Indeed, the unusual hot at dry meteorological conditions of 2006 could impact the values of the calibrated parameters and, thus, the estimations of biomasses. An analysis of the optimal dataset combining optimal FORMOSAT-2 time series and representative meteorological conditions should be further investigated. Secondly, in the SAFY model, the ELUE is constant all over the phenological cycle, which could lead to errors in the dry aboveground biomass estimations especially during the senescence phase as shown by Lecoeur et al. (2011) for sunflower. A temporal variation of ELUE after flowering might be investigated.

Finally, inter-annual variation in grain yields over the entire Formosat-2 data set of images (24 \( \times \) 24 km\(^2\)) was estimated using maize and sunflower and compared with grain yield statistics given by the French Agricultural Statistics for the entire department of Haute-Garonne (6300 km\(^2\)). The SAFY model was able to correctly reproduce the inter-annual variation in the grain yield of sunflower (\( r^2 = 0.89 \)). In contrast, the inter-annual variation of maize grain yield was not correctly reproduced because of the lack of spatial representativeness of our simulations. Indeed, contrary to the sunflower crops, the FORMOSAT-2 footprint was not representative of the maize behaviours encountered over the whole department.

This study demonstrates the great potential for the use of high spatial and temporal resolution remote sensing data for large-scale crop monitoring. Future satellite missions such as Vénus (Dedieu et al., 2006) and Sentinel-2, which will provide high spatial and temporal resolution images with a 4/5 days revisiting period and with a high number of spectral bands (12/13 spectral bands), will offer new perspectives for such applications.

Acknowledgements

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Appendix A. Overview of the SAFY model

The simple algorithm for yield estimates (SAFY, Duchemin et al., 2006b) is a daily time-step model that simulates time series of leaf area index (LAI) and dry aerial mass (DAM) from the air temperature (Ta) and the global incoming radiation (Rg). The simulations begin on the plant emergence day (D0). \( D_0 \) depends on agricultural practices (in particular sowing date and depth) and on the pedoclimatic conditions and constrains the phase of the LAI time course.

Daily DAM production (\( \Delta_{DAM} \)) is calculated through the approach of Monteith (1977, Eq. (2)) using an effective light-use efficiency (ELUE), a daily temperature stress factor (FT) and the daily photosynthetically active radiation absorbed by plants (APAR). The ELUE expresses the conversion of the APAR into DAM. It is supposed to account for all agri-environmental stresses, such as water and nitrogen supplies, except for temperature. It constrains the amplitude of the GAI time course. The temperature stress function is a classical Polynomial (Eq. (3)) of \( \beta \) Degree defined by an optimal daily mean air temperature (Topt) for maximum crop functioning and two extreme temperatures (Tmin and Tmax) beyond which the plant growth stops (after Brisson et al., 2003). The APAR (Eq. (4)) is computed using the daily incoming global radiation (Rg), the climatic efficiency (EC) and the fraction of the photosynthetically active portion of solar radiation absorbed by green plants (FAPAR). In the SAFY model, the FAPAR is estimated using Beer’s law (Eq. (5)), where kSLA defines the light-extinction coefficient (Monsi and Saeki, 1953).

\[
\Delta_{DAM} = ELUE \times FT \times APAR
\]  
\[F_T(Ta) = 1 - \left( \frac{T_{opt} - Ta}{Topt - Tmin} \right)^\beta \quad \text{if} \quad Tmin < Ta < Topt
\]  
\[F_T(Ta) = 0 \quad \text{if Ta} > T_{max} \quad \text{OR} \quad Ta > T_{opt}
\]  
\[APAR = FAPAR \times EC \times Rg
\]  
\[FAPAR = 1 - e^{-k_{SLA} \times LAI}
\]

During plant growth, a fraction of the daily plant DAM production is partitioned to the dry leaf biomass. This fraction is calculated using the partition-to-leaf function Pl (Eq. (6), after Maas, 1993), which varies from 0 to 1. Pl is a function of the daily air temperature cumulated from plant emergence (SMT: sum of temperature, Eq. (7)) and two parameters: Pla and Plb. It should be noted that (1 – Pla) defines the rate of biomass allocation to leaves at plant emergence. Daily leaf mass production (\( \Delta_{DAM} \times Pl \)) is converted into daily leaf area growth (\( \Delta_{LAI} \)) based on the specific leaf area (SLA, Eq. (8)). Leaf senescence (\( \Delta_{LAI} \)) begins when the SMT reaches a given threshold (Stt, sum of temperature for senescence). It is modelled by a function (Eq. (9)) based on the rate of senescence coefficient (Rs). The LAI is updated from the balance of \( \Delta_{LAI} \) and \( \Delta_{LAI} \) (Eq. (10)).

\[
PL = 1 - PL \times e^{-PLa \times SMT}
\]
\[
SMT = \int_{0}^{t} (Ta - Tmin) \, dt
\]
\[
If \; Pl > 0, \Delta_{LAI} = \Delta_{DAM} \times Pla
\]
\[
If \; SMT > Stt, \Delta_{LAI} = LAI \times \frac{SMT - Stt}{Rs}
\]
\[
LAI_{t+1} = LAI_t + \Delta_{LAI} - \Delta_{LAI}
\]

References


